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**Relation Visualization of Environmental Quality Index with Environmental Resource Indicators Using Multiple Indicators Multiple Causes Model**

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**Abstract**

This research aims to visualize the model of environmental resource factors on the constituent factors of the environmental quality index using the multiple indicators multiple causes (MIMIC) method, using secondary data sourced from IKLH 2020. The predictor variables in this study include air quality, water quality, land cover quality, and environmental quality. Some of the indicators in this research are Conservation Forest Area, Limited Production Forest Area, Fixed Production Forest Area, Protection Forest Area, Coral Reefs, and Mangroves. Data Analysis using MIMIC Model generated by JASP Software, showing a very significant baseline and model factor. Some predictor coefficients have low standard error (close to zero), as well as significant indicators coefficients, except coral reefs, with a p-value of 0.736. The form model is worth using, since the RMSEA is worth 0.188. With a P-Value of 0.005. A high R-Squared is given by two indicators, namely Limited Production Forest Area, and Fixed Production Forest Area, respectively valued at 0.968 and 0.790.

**Keywords:** MIMIC Model, Environmental Resources, Environmental Quality Indices, Math Modelling

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**Introduction**

Multiple Indicators Multiple Causes Model known as one of flexible model in statistics. MIMIC models are useful in that they can be used for continuous, categorical, or mixes of continuous and categorical outcomes. Throughout this manuscript we provide examples and equations for dichotomous outcomes only. Because MIMIC models are estimated in a SEM framework model fit indices (RMSEA, SRMR, Hoelter's Critical, GFI, MFI, ECVI) are available for these models. However, many models fit statistics are only valid for model with continuous outcomes [1]. Montoya and Joen note that though conceptualizing uniform and non-uniform DIF MIMIC models within a mediation and moderation framework can be very

useful, we caution against using this framework to make causal inferences without thoroughly investigating the assumptions needed to do so [2].

The MIMIC model is the most popular method used to detect DIF in recent studies, such as research conducted by Finch [3], Shih & Wang [4], Finch & French [5], and Cheng, Shao & Lathrop [6]. In Statistical Procedure, The Multiple Indicators Multiple Causes (MIMIC) model has several criteria namely, Model fitting indices indicate the good establishments of the MIMIC model of sustainable development indicators, where  $\chi^2/df$  is less than 1, the RMSEA is less than 0.05, and the values of the goodness of fit index (GFI), the comparative fit index (CFI), and the Tucker–Lewis index (TLI) were greater than 0.9. (Dehghani, et al, 2023).

The MIMIC Model Formulation [8]:

$$\eta = Y_1X_1 + Y_2X_2 + \dots + Y_qX_q + \zeta \quad (1)$$

$$y_1 = \lambda_1\eta + \varepsilon_1;$$

$$y_2 = \lambda_2\eta + \varepsilon_2;$$

(...)

$$y_p = \lambda_p\eta + \varepsilon_p. \quad (2)$$

## Method

This research aims to visualize the model of environmental resource factors on the constituent factors of the environmental quality index using the multiple indicators multiple causes (MIMIC) method, using secondary data sourced from Indeks Kualitas Lingkungan Hidup (IKLH) at 2020. This Research focused to explore IKLH of Provinces in four Islands in Indonesia (Java Island, Sumatra Island, Borneo Island, and Sulawesi Island). The predictor variables in this study include air quality, water quality, land cover quality, and environmental quality. Some of the indicators in this research are Conservation Forest Area, Limited Production Forest Area, Fixed Production Forest Area, Protection Forest Area, Coral Reefs, and Mangroves. Data Analysis using MIMIC Model generated by JASP Software:

$$Y \sim \lambda_1 * \text{Conservation\_Forest} + \lambda_2 * \text{Limited\_Production\_Forest} + \lambda_3 * \text{Fixed\_Production\_Forest} + \lambda_4 * \text{Protection\_Forest} + \lambda_5 * \text{Coral\_Reefs} + \lambda_6 * \text{Mangrove}$$

$$Y \sim \beta_1 * \text{Air\_Quality} + \beta_2 * \text{Water\_Quality} + \beta_3 * \text{Land\_Cover\_Quality} + \beta_4 * \text{Environmental\_Quality}$$

**Result**

This research analysis given in Table 1 – Table 7 and also Figure 1. Data Analysis using MIMIC Model generated by JASP Software, showing a very significant baseline and model factor. Some predictor coefficients have low standard error (close to zero), as well as significant indicators coefficients, except coral reefs, with a p-value of 0.736. The form model is worth using, since the RMSEA is worth 0.188. With a P-Value of 0.005. A high R-Squared is given by two indicators, namely Limited Production Forest Area, and Fixed Production Forest Area, respectively valued at 0.968 and 0.790.

**Table 1. Chi Square Test**

	df	$\chi^2$	p
Baseline model	45	311.023	0.000
Factor model	29	55.536	0.002

**Table 2. Predictors Coefficients**

Predictor	Estimate	Std. Error	z-value	p	95% Confidence Interval		Standardized		
					Lower	Upper	All	LV	Endo
Kualitas_Udara	0.070	0.102	0.685	0.493	-0.130	0.270	0.358	0.060	0.060
Kualitas_Air	0.138	0.105	1.312	0.190	-0.068	0.343	0.876	0.118	0.118
Kualitas_Tutupan_Lahan	0.180	0.142	1.269	0.204	-0.098	0.459	2.719	0.155	0.155
Kualitas_Ljngkungan_Hidup	-0.362	0.339	-1.067	0.286	-1.026	0.303	-2.960	-0.310	-0.310

**Table 3. Indicators Coefficients**

Indicator	Estimate	Std. Error	z-value	p	95% Confidence Interval		Standardized		
					Lower	Upper	All	Latent	Endo
Hutan_Konservasi	107.253	43.687	2.455	0.014	21.629	192.878	0.461	125.159	0.461
Hutan_Produksi_Terbatas	973.494	144.863	6.720	$1.816 \times 10^{-11}$	689.567	1257.420	0.984	1136.020	0.984
Hutan_Produksi_Tetap	846.072	147.684	5.729	$1.011 \times 10^{-8}$	556.617	1135.526	0.889	987.324	0.889
Hutan_Lindung	517.210	103.263	5.009	$5.480 \times 10^{-7}$	314.819	719.601	0.815	603.559	0.815
Terumbu_Karang	5.162	15.288	0.338	0.736	-24.802	35.126	0.067	6.024	0.067
Mangrove	27.926	7.837	3.563	$3.662 \times 10^{-4}$	12.565	43.286	0.633	32.588	0.633

**Table 4. Fit Indices**

Index	Value
Comparative Fit Index (CFI)	0.900
Tucker-Lewis Index (TLI)	0.845
Bentler-Bonett Non-normed Fit Index (NNFI)	0.845
Bentler-Bonett Normed Fit Index (NFI)	0.821
Parsimony Normed Fit Index (PNFI)	0.529
Bollen's Relative Fit Index (RFI)	0.723
Bollen's Incremental Fit Index (IFI)	0.906
Relative Noncentrality Index (RNI)	0.900

Table 5. Information Criteria

	Value
Log-likelihood	-1428.527
Number of free parameters	26.000
Akaike (AIC)	2909.054
Bayesian (BIC)	2942.745
Sample-size adjusted Bayesian (SSABIC)	2861.974

Table 6. RMSEA and Other Fit Measures

Metric	Value
Root mean square error of approximation (RMSEA)	0.188
RMSEA 90% CI lower bound	0.111
RMSEA 90% CI upper bound	0.262
RMSEA p-value	0.005
Standardized root mean square residual (SRMR)	0.134
Hoelter's critical N ( $\alpha = .05$ )	20.924
Hoelter's critical N ( $\alpha = .01$ )	24.215
Goodness of fit index (GFI)	0.754
McDonald fit index (MFI)	0.600
Expected cross validation index (ECVI)	4.136

Table 7. R - Squared

	R <sup>2</sup>
Hutan_Konservasi	0.213
Hutan_Produksi_Terbatas	0.968
Hutan_Produksi_Tetap	0.790
Hutan_Lindung	0.664
Terumbu_Karang	0.004
Mangrove	0.401
Y	0.266

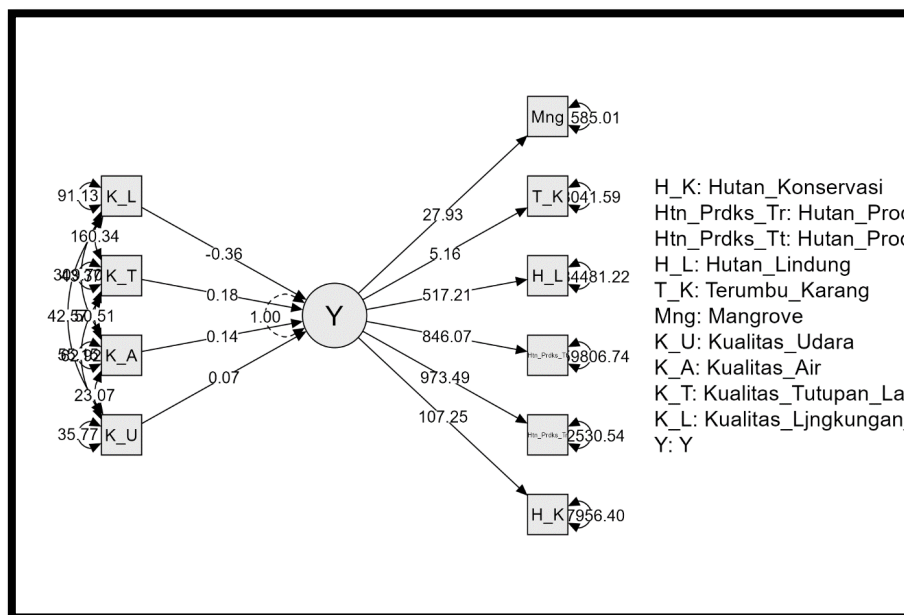


Figure 1. Visualize of MIMIC Model

## Conclusion

Based on path diagram of MIMIC model, so we can get the model of Environmental Quality Index with Environmental Resource Indicators Using Multiple Indicators Multiple Causes as:

$$Y \approx 107.253 * \text{Conservation\_Forest} + 973.494 * \text{Limited\_Production\_Forest} + 846.072 * \text{Fixed\_Production\_Forest} + 517.210 * \text{Protection\_Forest} + 5.165 * \text{Coral\_Reefs} + 27.926 * \text{Mangrove}$$

$$Y \sim 0.070 * \text{Air\_Quality} + 0.138 * \text{Water\_Quality} + 0.180 * \text{Land\_Cover\_Quality} - 0.362 * \text{Environmental\_Quality}$$

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